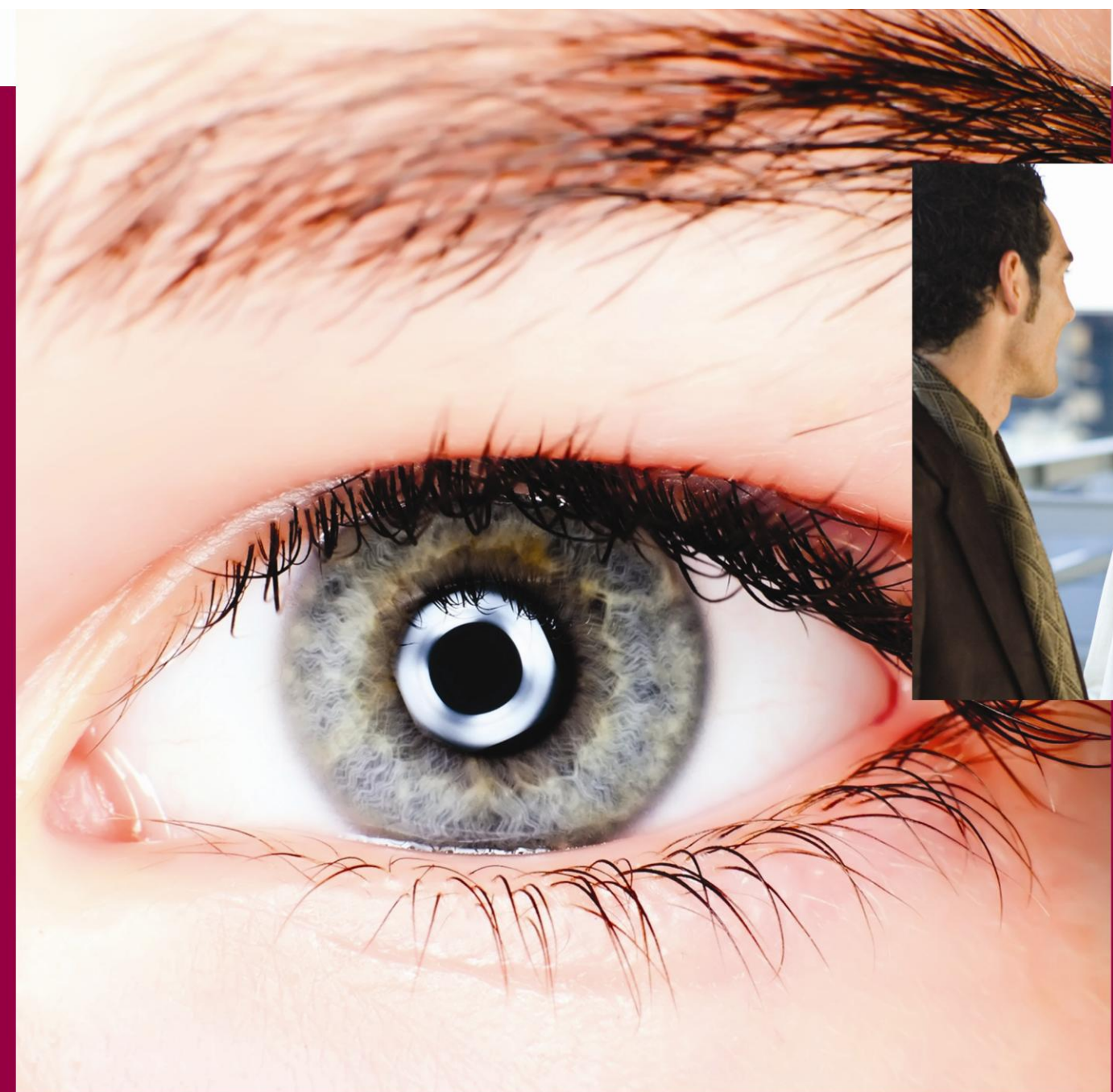


# Real Time Adaptive Face Recognition – Under the Hood



## Everyday Sensing and Perception

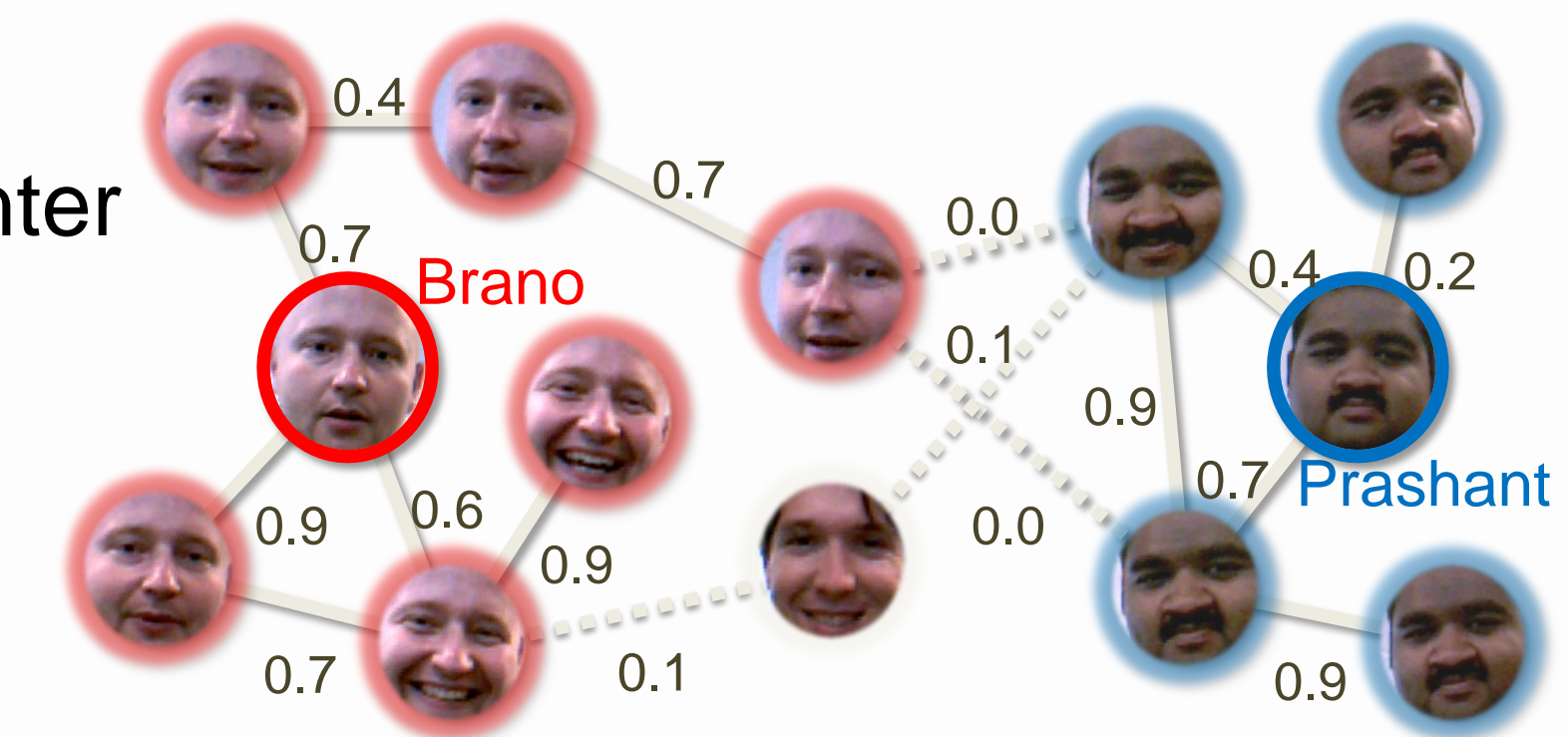
## REAL-TIME LEARNING WITHOUT EXPLICIT FEEDBACK

### Similarity Matrix

- Defined over set of faces, higher weights to the pixels in the center

$$w_{ij} = \exp \left[ -\frac{d^2(\mathbf{x}_i, \mathbf{x}_j)}{2\sigma^2} \right],$$

$$\text{where } d(\mathbf{x}_i, \mathbf{x}_j) = \min \left\{ \begin{array}{l} \|\mathbf{x}_i - \mathbf{x}_j\|_{2,\psi}, \\ \|(\mathbf{x}_i - \bar{\mathbf{x}}_i) - (\mathbf{x}_j - \bar{\mathbf{x}}_j)\|_{2,\psi}, \\ \|\mathbf{x}_i/\bar{\mathbf{x}}_i - \mathbf{x}_j/\bar{\mathbf{x}}_j\|_{2,\psi} \end{array} \right\}$$



### Online Algorithm

#### Inputs:

- an unlabeled example  $\mathbf{x}_t$
- a quantized data adjacency graph  $W_{t-1}$
- vertex multiplicities  $\mathbf{v}_{t-1}$

#### Algorithm:

- if the graph  $W_{t-1}$  has less than  $n_g$  vertices
  - add a new vertex  $\mathbf{x}_t$  to the graph  $W_{t-1}$
  - $v_t(l) = v_{t-1}(l)$  for  $l = 1, \dots, t-1$
  - $v_t(t) = 1$
- else
  - find the vertices  $i$  and  $j$  that minimize  $v_{t-1}(j)d(\mathbf{x}_i, \mathbf{x}_j)$
  - replace the  $j$ -th vertex of the graph  $W_{t-1}$  with  $\mathbf{x}_t$
  - $v_t(l) = v_{t-1}(l)$  for  $l = 1, \dots, n_g$
  - $v_t(i) = v_{t-1}(i) + v_{t-1}(j)$
  - $v_t(j) = 1$
- $W_t = W_{t-1}$
- $\hat{W}_t = V_t W_t V_t$
- compute the Laplacian  $\hat{L}$  of the graph  $\hat{W}_t$
- infer labels on the graph:
  - $\hat{\ell} = \arg \min_{\ell} \ell^T (\hat{L} + \gamma_g V_t) \ell$
  - s.t.  $\ell_i = y_i$  for all labeled examples up to the time  $t$
- make a prediction  $\hat{y}_t = \text{sgn}(\hat{\ell}_t)$

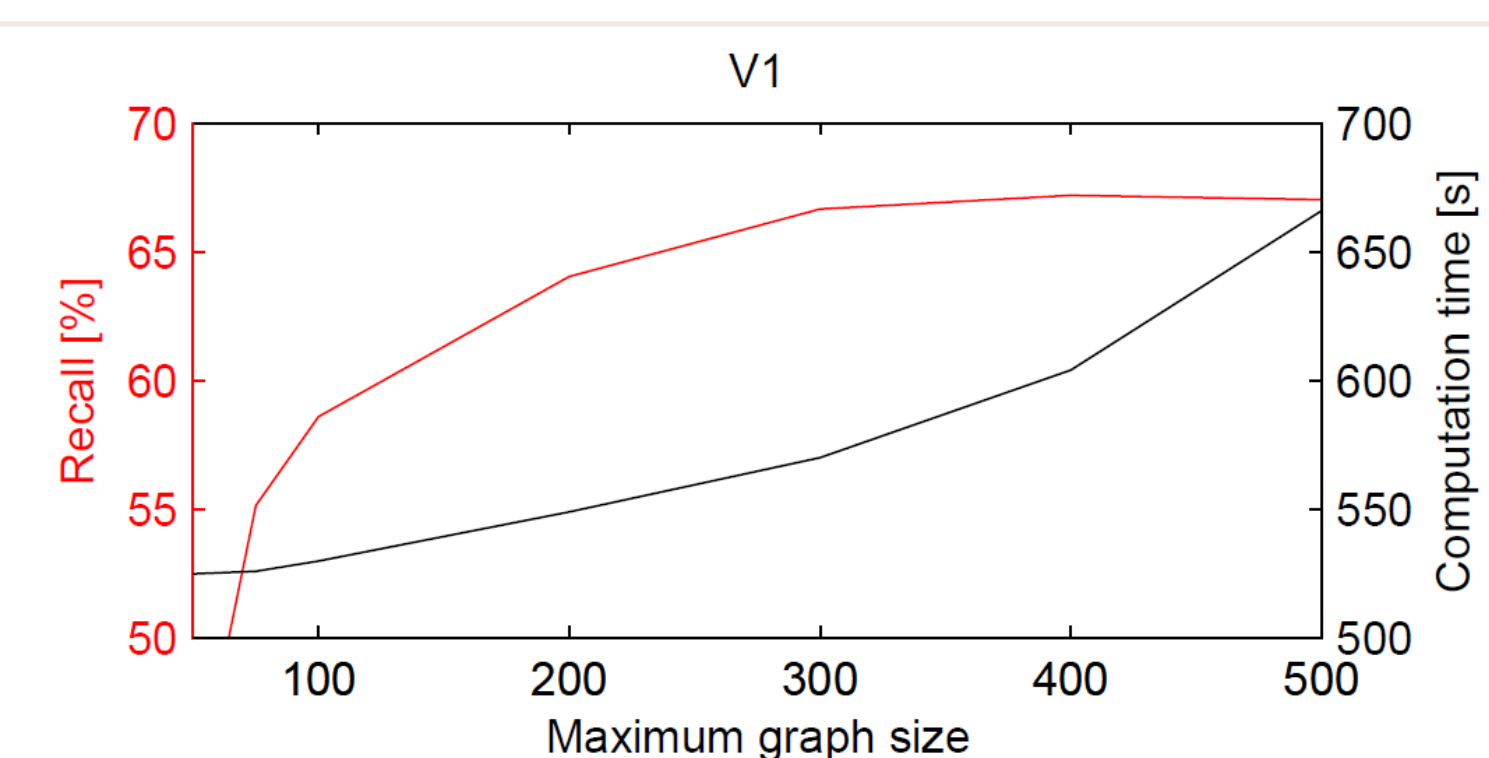
#### Outputs:

- a prediction  $\hat{y}_t$
- a quantized data adjacency graph  $W_t$
- vertex multiplicities  $\mathbf{v}_t$

Online harmonic function solution at the time step  $t$ . The main parameters of the algorithm is the regularizer  $\gamma_g$  and the maximum number of vertices  $n_g$ .

### Data Quantization

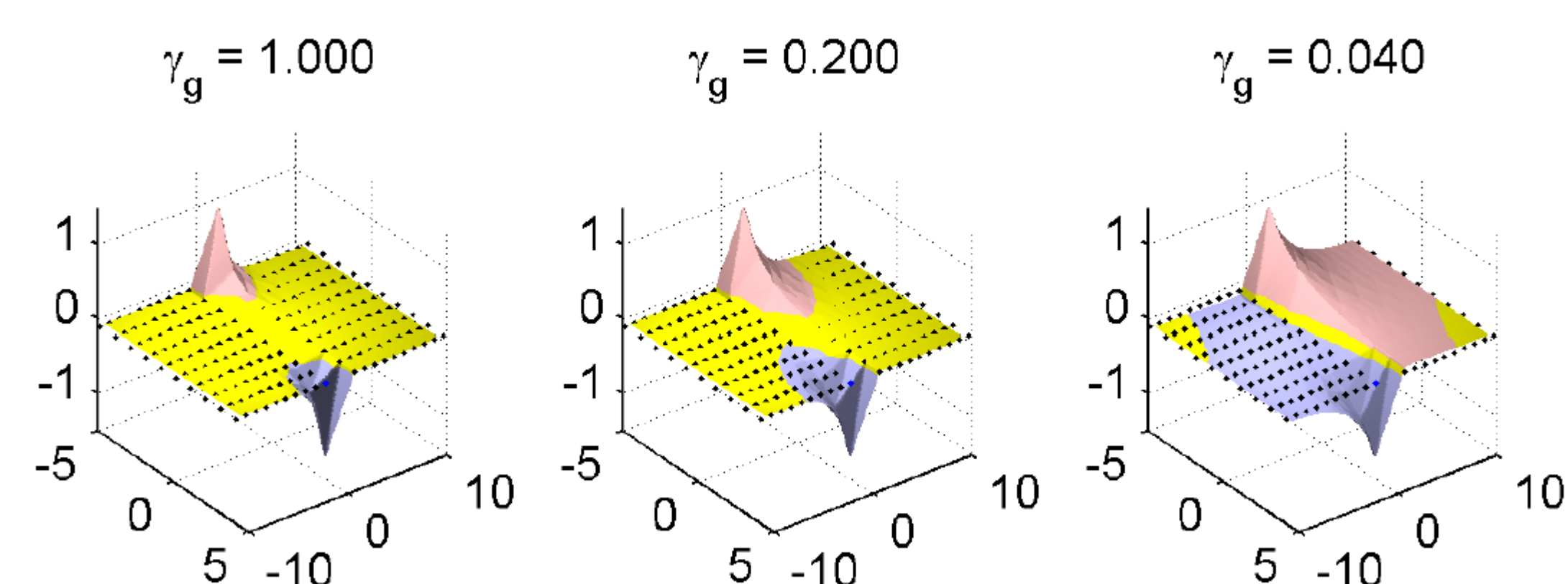
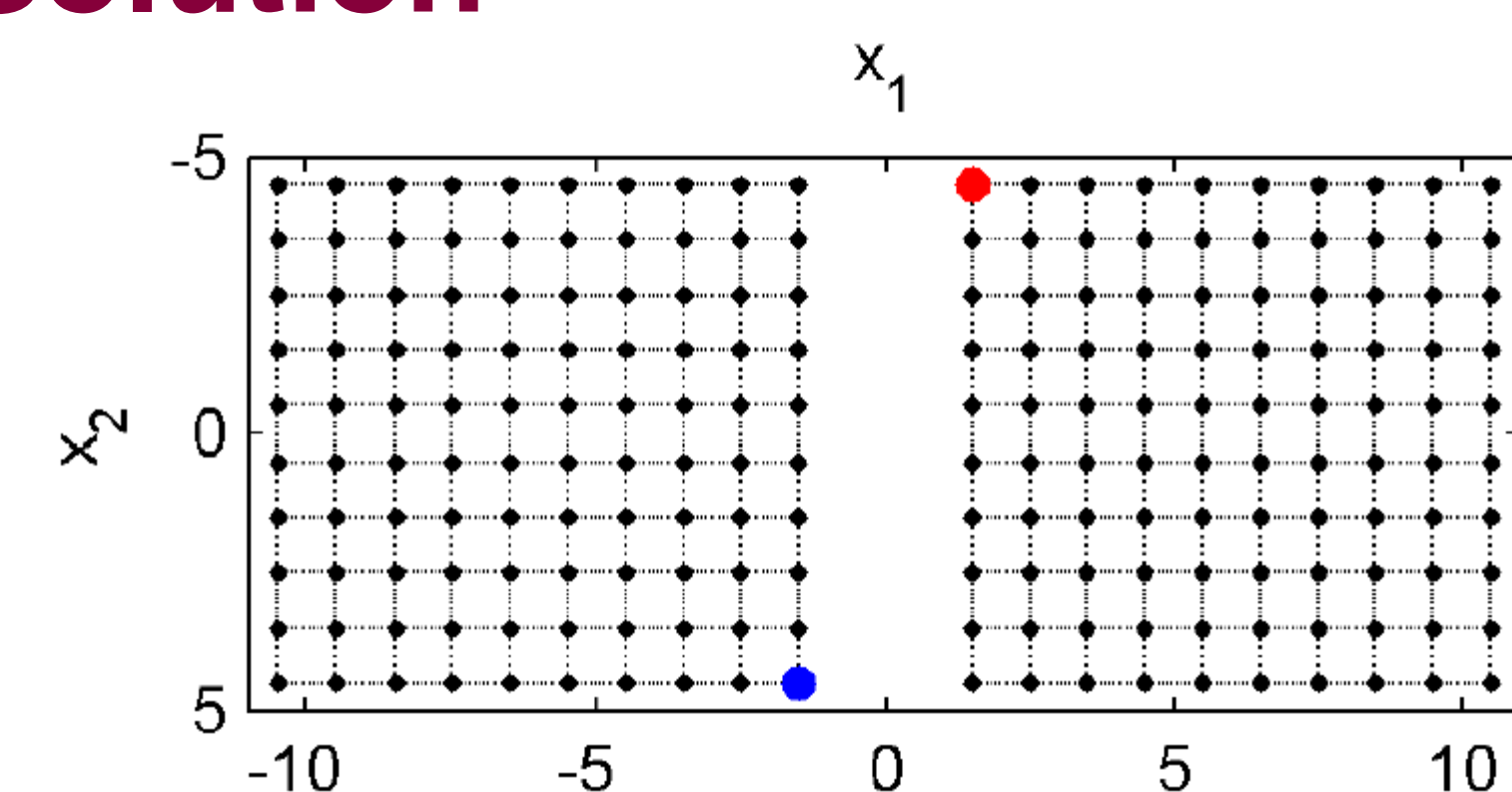
- Cannot store all the past data
- Similarity graph needs to be reasonably small
- Greedily find the closest pair of nodes
- Represent the two nodes by a single one
- Keep track of *multiplicities*



$$\hat{\ell}_u = (\hat{L}_{uu} + \gamma_g V)^{-1} \hat{W}_{ul} \ell_l$$

### Regularized Harmonic Solution

Minimum satisfies the harmonic property and has a closed form solution.



Regularization controls the amount of extrapolation to unlabeled data. The lower the regularizer, the more we trust unlabeled data

### Prediction Error Analysis

$$\frac{1}{n} \sum_t (\hat{\ell}_t - y_t)^2 \leq \frac{9}{2n} \sum_t (\hat{\ell}_t - \tilde{\ell}_t)^2 + \frac{9}{2n} \sum_t (\tilde{\ell}_t - \ell_t^*)^2 + \frac{9}{2n} \sum_t (\ell_t^* - y_t)^2.$$

Quality of quantization

Difference between the offline and online prediction

$O(\sqrt{n})$  by the algorithm stability argument of [Cortes et al. 2008]