



Graphs in Machine Learning

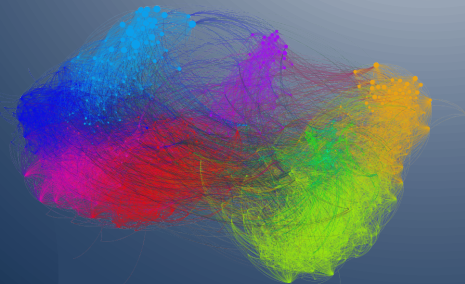
Spectral Clustering: Examples

Understanding and Applications

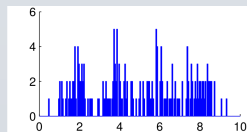
Michal Valko

Inria & ENS Paris-Saclay, MVA

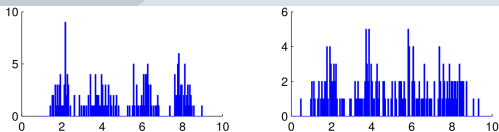
Partially based on material by: Ulrike von Luxburg,
Gary Miller, Doyle & Schnell, Daniel Spielman



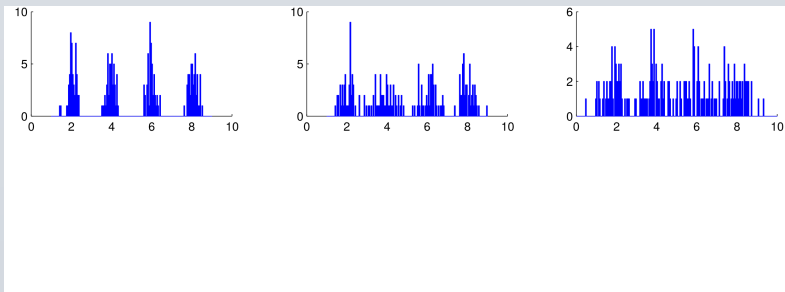
Spectral Clustering: 1D Example



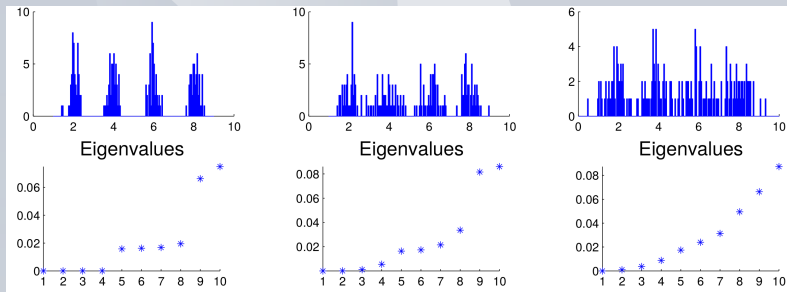
Spectral Clustering: 1D Example



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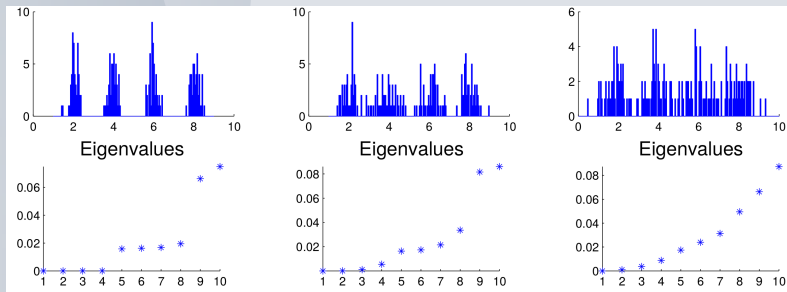


Spectral Clustering: 1D Example



Spectral Clustering: 1D Example

Elbow rule/EigenGap heuristic for number of clusters

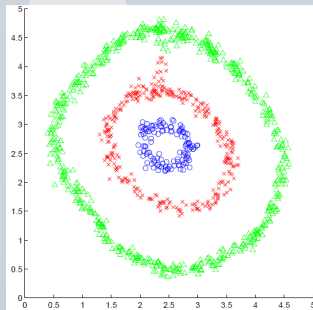
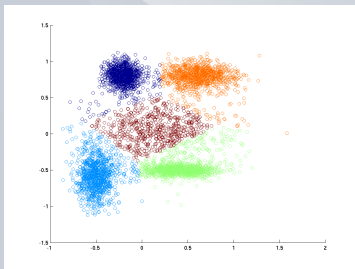


Spectral Clustering: Understanding

Compactness vs. **Connectivity**

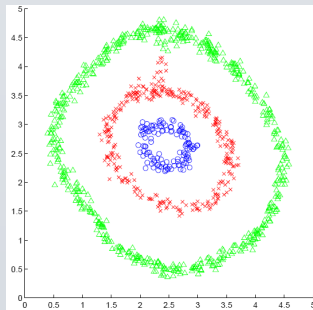
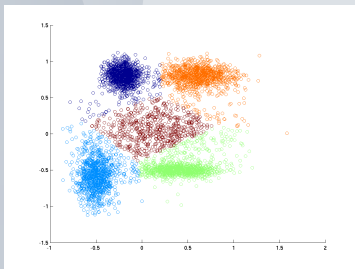
Spectral Clustering: Understanding

Compactness vs. Connectivity



Spectral Clustering: Understanding

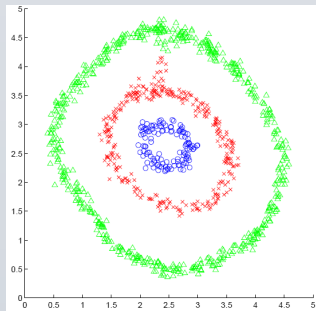
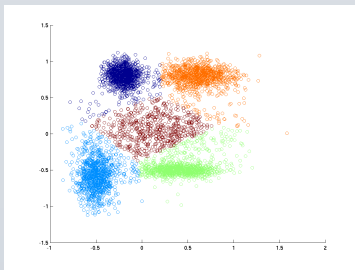
Compactness vs. Connectivity



For which kind of data we can use one vs. the other?

Spectral Clustering: Understanding

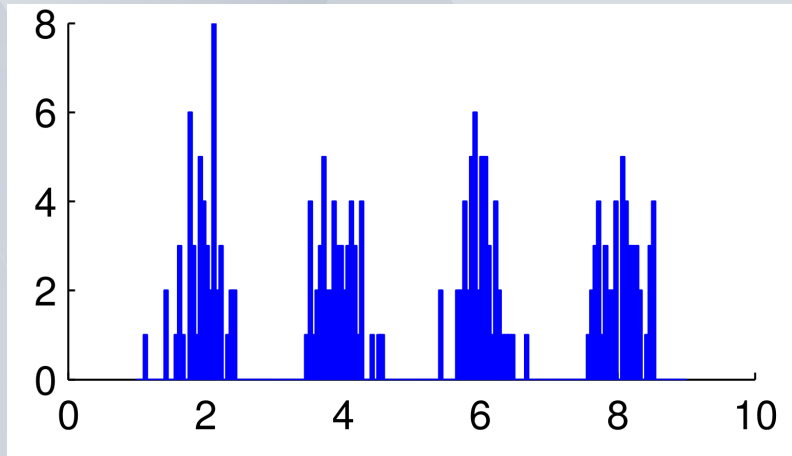
Compactness vs. Connectivity



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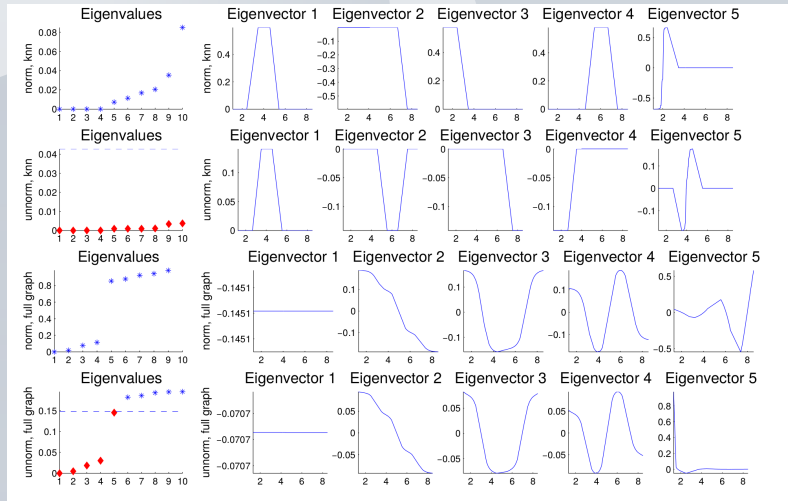
Any disadvantages of spectral clustering?

Spectral Clustering: 1D Example - Histogram



http://www.informatik.uni-hamburg.de/ML/contents/people/luxburg/publications/Luxburg07_tutorial.pdf

Spectral Clustering: 1D Example - Eigenvectors



Spectral Clustering: Bibliography

- **meila2001random**
- L_{sym} **ng2001spectral**
- L_{rm} **shi2000normalized**
- Things can go wrong with the relaxation:
spielman2007spectral

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`https://misovalko.github.io/mva-ml-graphs/`