



# Graphs in Machine Learning

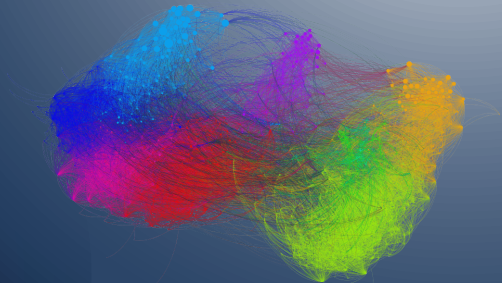
## Google PageRank: Introduction

Random Surfer Model

Michal Valko

*Inria & ENS Paris-Saclay, MVA*

Partially based on material by: Andreas Krause,  
Branislav Kveton, Michael Kearns



## Success story #2 Google PageRank

*Objective:* **Rank** all web pages (nodes on the graph) by how **many** other pages link to them and how **important** they are.

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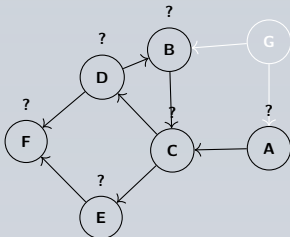
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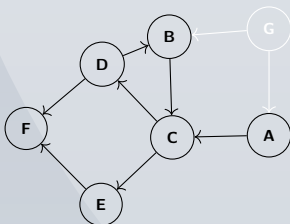


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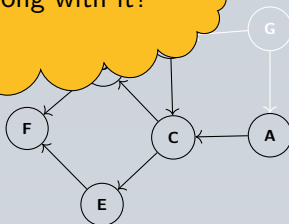
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**Random Surfer Process**

basic PageRank is in fact a **stochastic** process

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What is wrong with it?



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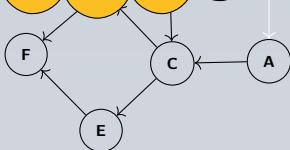
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basic PageRank is in fact a simple iterative

Internet  $\rightarrow$  graph  $\rightarrow$  matrix  $\rightarrow$  rank  
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*PageRank can be thought of as a model of user behavior. We assume there is a “random surfer” who is given a web page at random and keeps clicking on links, never hitting “back” but eventually gets bored and starts on another random page.*

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  - circular definition
- importance of a page is distributed **evenly**
- probability of being bored is 15%





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`https://misovalko.github.io/mva-ml-graphs.html`